

# Notes on New Method for Calculating NRR Assessor Sensitivity

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We are dealing with a curve where a measure  $m$  is calculated for increasing magnitudes of perturbation/misregistration,  $d$ . At each level of misregistration  $d_i$  we have one particular value of  $m$ , with corresponding standard error,  $\sigma_i$ .

As well as this standard error which is related to the number of samples we use to measure  $m$  (the uncertainty in the measure), we have another uncertainty, due to repetition, or separate “trials”.

$i \leftarrow m_i$ , i.e. the index  $i$  is related to the measures whereas, on the other hand,  $j$  indexes the trials.  $m_{ij}$  is the measure at one particular point for a particular trial and  $S$  (or  $D$  in prior papers), the sensitivity of the measure, is what we seek to identify.

To measure the mean of  $m$ , we use the summation thus

$$\bar{m}_i = \sum_j^N \frac{m_{ij}}{N}.$$

And the errors are summarised in a messy fashion in the sets of equations below.

$$\begin{aligned} \sigma_{\bar{m}_i} &= \frac{\sigma_{m_{ij}}}{\sqrt{N}} \\ \sigma_{\sigma_{\bar{m}_i}} &= \frac{\sigma_{m_{ij}}}{\sqrt{2N}} \\ \sigma_{\bar{m}_{ij}} &\pm \sigma_{\sigma_{\bar{m}_{ij}}} \end{aligned}$$

$$\begin{aligned} &\sqrt{\sum_j^n \sigma_{\sigma_{\bar{m}_i}}^2} \\ &S + \sigma_s \\ &\langle \bar{\sigma}_{\bar{m}_i} \rangle \langle \bar{\sigma}_{\sigma_{\bar{m}_i}} \rangle \end{aligned}$$

$N$  is the number of repeated experiments, among the instantiations that we have.

We fit a function to the measures curve (e.g. Specificity or overlap) and its error bars and then compute the ratio of the curve over the mean of all inter-instantiation error bars. Error should be added and aggregated too, in lines with some of the rules above.